

## Lecture 2: The neo-classical model of international trade

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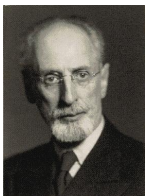
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Eco 572, International Economics

September 22<sup>nd</sup>, 2010

# Class Overview

1. The HOS model
2. Openness and income inequalities : the Stolper-Samuelson theorem
3. The role of factor endowments : the Rybczynski theorem
4. The Leontieff paradox



**Eli Heckscher**  
(1879-1952)

*The Effect of Foreign  
Trade on the Distribu-  
tion of Income, 1919*



**Bertil Ohlin**  
(1899-1979)

*Interregional and Inter-  
national Trade, 1933*



**Paul Samuelson**  
(1915- )

*Foundations of Econo-  
mics Analysis, 1947*

# The HOS Model

# Overview

- **Assumptions**

- 2 countries, 2 goods, 2 production factors ( $2 \times 2 \times 2$ )
- Factors are mobile across sectors but immobile across countries
- Free trade, no transportation costs

- **Results**

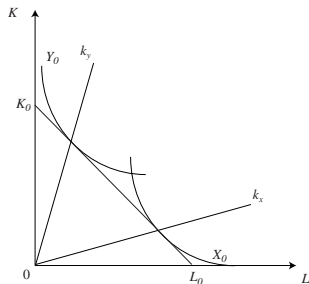
- Origin of comparative advantages
- Specialization raises social welfare but unequally across individuals

# The Model

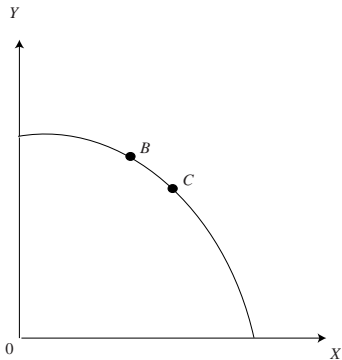
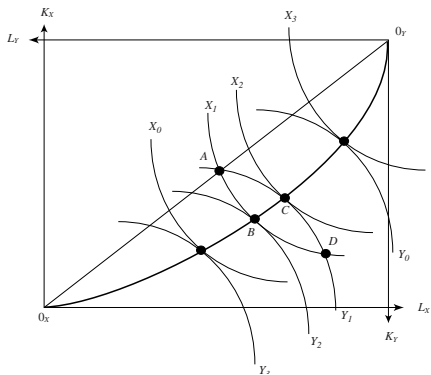
- 2 countries : Home and Foreign (\*)
- 2 goods : X (labor intensive), Y (capital intensive)
- 2 factors : K, L, mobile across sectors (hence same factor prices)
- Technical coefficients  $L/Y$ ,  $K/Y$  depend on relative factor prices  $w/r$  (substitutability)
- Same production functions in both countries
- Home relatively richer in capital than in labor, compared to Foreign :  
 $(K/L) > (K^*/L^*)$
- Equilibrium of factor markets :  
Labor :  $L_X + L_Y = L$   
Capital :  $K_X + K_Y = K$   
Same in the foreign country ( $K^*$ ,  $L^*$ )
- Perfect competition  
→ Zero profit in equilibrium
- Budget constraint :  
 $Y = wL + rK$

# Factor intensity

- 2 goods :  $X = F_X(L_X, K_X)$  and  $Y = F_Y(L_Y, K_Y)$
- $X$  is relatively labor intensive :  $\frac{K_Y}{L_Y} > \frac{K_X}{L_X}$
- Isoquant : Combinations of  $L$  and  $K$  that give the same quantity of output
- At the firm's optimum, marginal rate of transformation = relative price of factors
- Mobility of factors across sectors  $\rightarrow$  MRT equalized

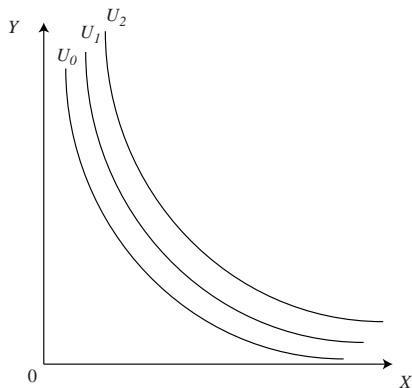


# Edgeworth box and the PPF



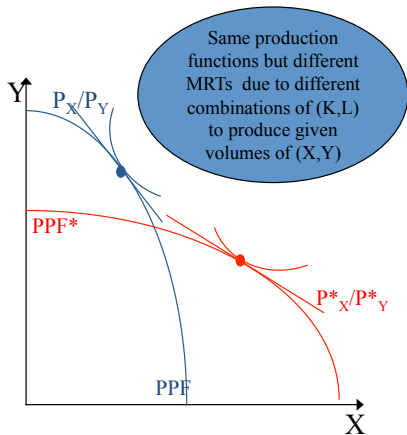


## Demand side

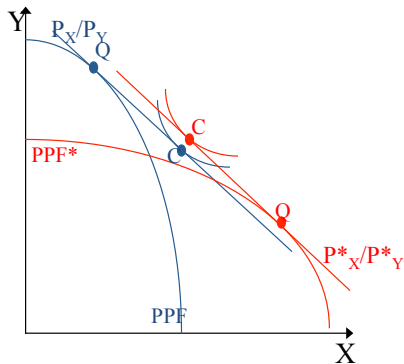


- On an indifference curve,  $MRS = -\frac{dY}{dX} = \frac{\partial U/\partial X}{\partial U/\partial Y}$
- At the consumer's optimum :  $\frac{P_X}{P_Y} = MRS$

## Autarky



## Open economy



# Opening to Trade

- **Autarky** :  $P_X/P_Y > P_X^*/P_Y^*$
- **Open economy** : Home starts importing  $X$  and Foreign starts importing  $Y$
- ⇒ Increased demand of  $Y$  in Home and of  $X$  in Foreign → Price convergence :  $P_X/P_Y \downarrow$ ,  $P_X^*/P_Y^* \uparrow$
- ⇒ Relative production of  $Y$  increases in Home/decreases in Foreign → Increased relative demand for capital in Home/for labor in Foreign →  $w/r \downarrow$ ,  $w^*/r^* \uparrow$

## Equalization of factor prices

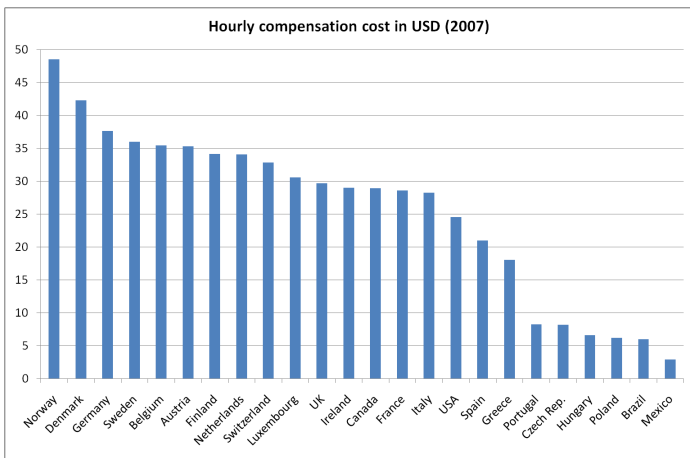
- Opening up the economy leads to **relative factor price equalization** across countries, even though factors are immobile internationally
  - In each sector, price = marginal cost + Across countries, prices equalize in each sector → Across countries, marginal costs equalize as well
  - Since production functions are the same in the two countries, the marginal cost is the same for each factor

- **Example :**

- $P_X = w^\alpha r^{1-\alpha} = w^{*\alpha} r^{*1-\alpha}$  and  $P_Y = w^\beta r^{1-\beta} = w^{*\beta} r^{*1-\beta}$
- Then :  $(w/r)^{\alpha-\beta} = (w^*/r^*)^{\alpha-\beta}$

⇒ **Heckscher-Ohlin-Samuelson theorem : “International trade leads to relative factor price equalization through international price equalization.”**

# Empirical evidence : No wage equalization



Source : US Bureau of Labor Statistics (August 2009)

# Limits

- No transport cost
- Impact of tariff and non-tariff barriers?
  - Perfect competition (hence price = marginal cost)
  - Homogeneous production functions across countries
  - Perfect mobility of factors across industries
  - Homogeneous production factors

# Openness and income inequalities : the Stolper-Samuelson theorem

# International trade and income inequalities

## **Stolper-Samuelson theorem :**

**“A rise in the relative price of a good increases the relative remuneration of the factor which is intensively used in the production of this good and reduces the remuneration of the other factor.”**

Hence opening up the economy leads to :

- A rise in the real remuneration of the relatively abundant factor
- A fall in the real remuneration of the relatively scarce factor

There are winners and losers :

- In Home, winners are the owners of physical and human capital
- In Foreign, winners are workers

Losers can theoretically be compensated through (preferably lump-sum) fiscal transfers from winners :

- In reality, physical and human capital is mobile internationally, which makes it difficult to tax them (tax competition)



# Demonstration

- Zero profit :

$$P_X X = wL_X + rK_X \quad \Rightarrow \quad P_X = wa_{LX} + ra_{KX}$$

$$P_Y Y = wL_Y + rK_Y \quad \Rightarrow \quad P_Y = wa_{LY} + ra_{KY}$$

with  $a_{LX} = L_X/X$ ,  $a_{KX} = K_X/X$ , etc.

- Differentiate  $P_X$  et  $P_Y$  for a given production structure (given  $a_{ij}$ ) :

$$dP_X = a_{LX}dw + a_{KX}dr$$

$$dP_Y = a_{LY}dw + a_{KY}dr$$

- Denote  $\theta_{KX} = a_{KX}r/P_X$  and  $\theta_{LX} = a_{LX}w/P_X$  (same for Y)

$$\frac{dP_X}{P_X} = \theta_{LX} \frac{dw}{w} + \theta_{KX} \frac{dr}{r} \quad \frac{dP_Y}{P_Y} = \theta_{LY} \frac{dw}{w} + \theta_{KY} \frac{dr}{r}$$

## Demonstration (2)

The evolution of factor prices then is :

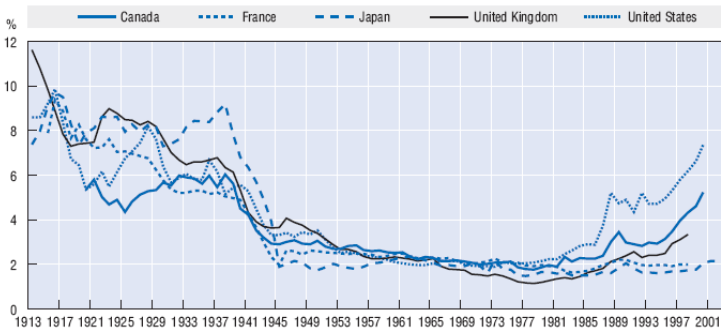
$$\frac{dw}{w} = \frac{\theta_{KY} \frac{dP_X}{P_X} - \theta_{KX} \frac{dP_Y}{P_Y}}{\theta_{KY}\theta_{LX} - \theta_{KX}\theta_{LY}} \quad \frac{dr}{r} = \frac{\theta_{LX} \frac{dP_Y}{P_Y} - \theta_{LY} \frac{dP_X}{P_X}}{\theta_{KY}\theta_{LX} - \theta_{KX}\theta_{LY}}$$

Since  $\theta_{KY} > \theta_{KX}$  (Y is more capital intensive) and  $\theta_{LX} > \theta_{LY}$  (X is more labor intensive), the denominator of both expressions is positive. It can be concluded that :

- if  $P_X$  (price of the relatively labor-intensive good) rises, then  $w$  (the remuneration of labor) increases while  $r$  (the remuneration of capital) falls
- if  $P_Y$  (price of the relatively capital-intensive good) increases, then  $w$  (the remuneration of labor) falls while  $r$  (the remuneration of capital) rises

# Trade openness and inequality

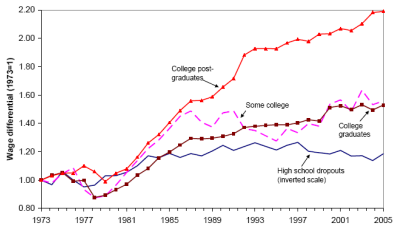
## Top 0.1% income share in 5 OECD countries, 1913-2001



Source: Piketty and Saez (2006).

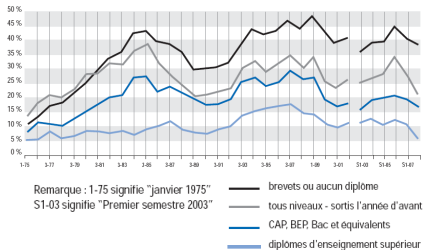
# Wage versus unemployment inequalities

## US : Hourly wage differentials relative to high school graduates (men)



Source : Lemieux (2008)

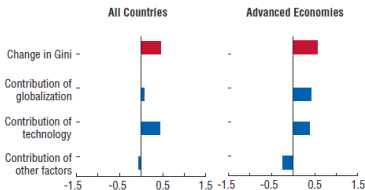
## France : Unemployment rate 1-4 years after exiting the education system



Source : INSEE

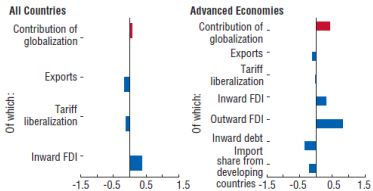
# Explaining changes in income inequalities

## Regression of Gini coefficient on globalization and technology-related variables



*Average annual % change of Gini coefficient*

## Decomposition of globalization effects on inequality

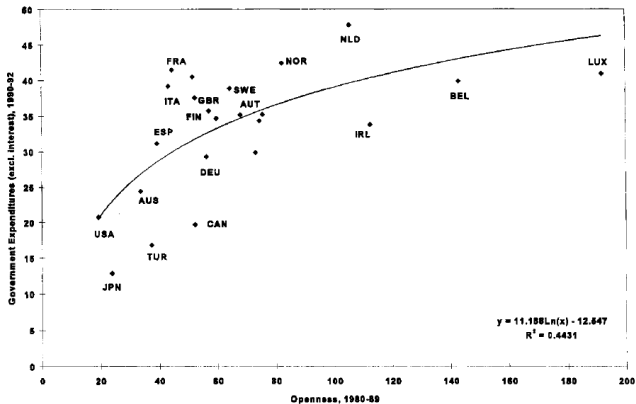


*Average annual % change of Gini coefficient*

Source : IMF, World Economic Outlook

# Compensating the Losers

## Trade openness and public expenditures



Source : D. Rodrik (1998)

# The role of factor endowments : the Rybczynski theorem

## Changes in factor endowments

**Rybczynski theorem** : *“For a given relative price, a higher endowment in one factor makes the production that uses this factor more intensively increase and the production that uses it less intensively decrease”*

**Consequences for a small economy** (exogenous prices) :

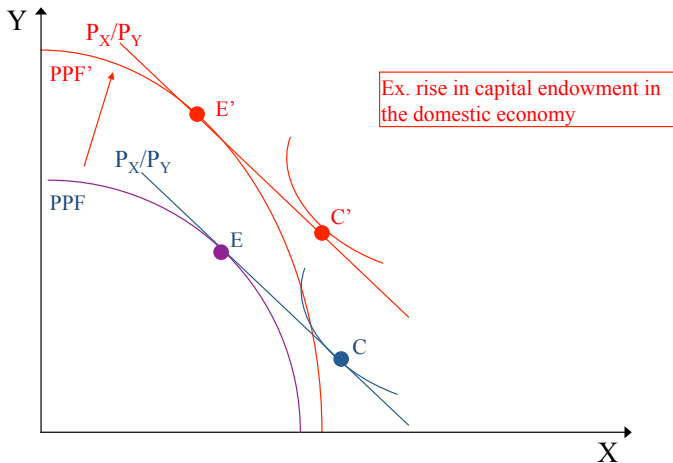
A rise in factor endowment is necessarily beneficial because the country can either :

- Export more, hence import more and consume more (export-biased growth) ;
- Import less, export less, but consume more (import-substitution growth)

Comparative advantages can change over time. Ex. Japan, China, Vietnam.



# The Rybczynski theorem

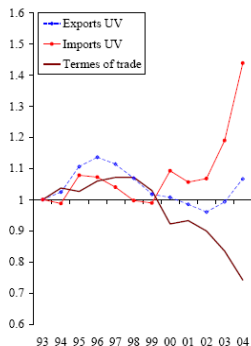


## Limits

In a **big country**, prices are endogenous :

- Export-biased growth deteriorates terms of trade, which may offset the positive impact of higher endowment = "impoverishing growth". Ex. China.
- Justification to import-substitution policies

## Terms of Trade in China



Source : Lemoine, 2007

# The Leontieff paradox

# The Leontieff paradox

## Leontieff (1953) :

- US exports are labor intensive  
 $K/L = 13,992$   
\$/person-year
- US imports (or, rather, US substitutes to imports) are more capital intensive  
 $K/L = 18,184$   
\$/person-year

Contradicts the theory of comparative advantage

## Possible explanations :

- Some imports have no substitute(ex. raw materials)
- Protection of labor-intensive industries
- Calculation should be based on bilateral trade
- Heterogeneity of factors (labor skills) or missing factors (land)
- Different technologies
- Limited inter-industry mobility
- Imperfect competition on goods and factor markets
- Vertical division of labor (exchange of tasks rather than goods).

# Other attempts to validate HOS

- **Heckscher-Ohlin-Vanek (1968)**

- Factoral content of exports should match world distribution of factors
- ex. Export of labor-intensive goods if  $L/L_{world} > Y/Y_{world}$

⇒ **Bowen, Leamer et Sveikaukas (1987)**

- 12 factors of production, 27 countries
- Fail to find "correct" ranking of countries

- **Trefler (1993, 1995)**

- 9 factors, 33 countries, year 1983
- 28% correlation between net factor exports and factor endowments
- problem : net exports are close to zero

# Conclusion

## At this stage, we have explained :

- why countries with different technologies and/or different production factor endowments trade with each other (ex : US and China)
- why different goods are being exchanged ("inter-industry trade")
- why openness to trade may increase wage inequality

## At this stage, we have not explained :

- why similar countries trade with each other (ex : France and Germany)
- why similar goods are being exchanged ("intra-industry trade")
- how/why labor and capital move across countries